



## A control benchmark on the energy management of a plug-in hybrid electric vehicle.

Antonio Sciarretta, Lorenzo Serrao, Prakash Chandra Dewagan, Paolino Tona, E.N.D. Bergshoeff, C. Bordons, E. Charmpa, P. Elbert, L. Eriksson, T. Hofman, et al.

### ► To cite this version:

Antonio Sciarretta, Lorenzo Serrao, Prakash Chandra Dewagan, Paolino Tona, E.N.D. Bergshoeff, et al.. A control benchmark on the energy management of a plug-in hybrid electric vehicle.. Control Engineering Practice, 2014, 29 (August), pp.287-298. 10.1016/j.conengprac.2013.11.020 . hal-01069628

HAL Id: hal-01069628

<https://ifp.hal.science/hal-01069628>

Submitted on 29 Sep 2014

**HAL** is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.

# A Control Benchmark on the Energy Management of a Plug-in Hybrid Electric Vehicle

A. Sciarretta<sup>a,\*</sup>, L. Serrao<sup>c,1</sup>, P.C. Dewangan<sup>a,e</sup>, P. Tona<sup>a</sup>,  
E.N.D. Bergshoeff<sup>h</sup>, C. Bordons<sup>i</sup>, L. Charmpa<sup>e,4</sup>, Ph. Elbert<sup>d</sup>, L. Eriksson<sup>f</sup>,  
T. Hofman<sup>h</sup>, M. Hubacher<sup>h</sup>, P. Isenegger<sup>h</sup>, F. Lacandia<sup>g,6</sup>, A. Laveau<sup>e,4</sup>,  
H. Li<sup>e,3</sup>, D. Marcos<sup>i</sup>, T. Nüesch<sup>d</sup>, S. Onorig<sup>7</sup>, P. Pisu<sup>b</sup>, J. Rios<sup>b</sup>, E. Silvas<sup>h</sup>,  
M. Sivertsson<sup>f</sup>, L. Triboli<sup>g,2</sup>, A.-J. van der Hoeven<sup>h</sup>, M. Wu<sup>e,3</sup>

<sup>a</sup>*IFP Energies nouvelles, France*

<sup>b</sup>*Clemson University, United States*

<sup>c</sup>*Dana Corp., Italy*

<sup>d</sup>*ETH Zurich, Switzerland*

<sup>e</sup>*IFP School, France*

<sup>f</sup>*Linköping University, Sweden*

<sup>g</sup>*Ohio State University, United States*

<sup>h</sup>*TU Eindhoven, The Netherlands*

<sup>i</sup>*University of Sevilla, Spain*

---

## Abstract

A benchmark control problem was developed for a special session of the IFAC Workshop on Engine and Powertrain Control, Simulation and Modeling (E-COSM 12), held in Rueil-Malmaison, France, in October 2012. The online energy management of a plug-in hybrid-electric vehicle was to be developed by the benchmark participants. The simulator, provided by the benchmark organizers, implements a model of the GM Voltec powertrain. Each solution

---

\*Corresponding author, holder of the Tuck Foundation Chair on Hybrid Vehicles and Energy Management: IFP Energies nouvelles, 1 et 4 avenue de Bois-Prau, 92852 Rueil-Malmaison Cedex, France, Fax: +33 147527012, email: antonio.sciarretta@ifpen.fr

<sup>1</sup>Previously with IFP Energies nouvelles, France.

<sup>2</sup>Also with University of Roma Tor Vergata, Italy. Currently with Tuscia University, Italy.

<sup>3</sup>Also with PSA, France. Currently with PSA, China.

<sup>4</sup>Also with Renault, France. Currently with Continental, France.

<sup>5</sup>Also with Continental, France. Currently with Continental, Germany.

<sup>6</sup>Also with University of Lecce, Italy.

<sup>7</sup>Currently with Clemson University, United States.

was evaluated according to several metrics, comprising of energy and fuel economy on two driving profiles unknown to the participants, acceleration and braking performance, computational performance. The nine solutions received are analyzed in terms of the control technique adopted (heuristic rule-based energy management vs. equivalent consumption minimization strategies, ECMS), battery discharge strategy (charge depleting–charge sustaining vs. blended mode), ECMS implementation (vector-based vs. map-based), ways to improve the implementation and improve the computational performance. The solution having achieved the best combined score is compared with a global optimal solution calculated off line using the Pontryagin's minimum principle-derived optimization tool HOT.

*Keywords:* Supervisory control, Plug-in Hybrid Electric Vehicles, Energy Management, Optimal Control, Rule-Based Control.

---

## 1. Introduction

Energy management of Hybrid Electric Vehicles (HEV) is nowadays a more-than-ten-years-old field of research in control engineering [1, 2, 3, 4, 5, 6, 7, 8, 9, 10]. Indeed, energy management is a control task since it consists in determining the setpoints (mostly, torque) to the various power converters (internal combustion engine, electric machines with their power electronics, mechanical transmission devices, electrical power converters, etc.) that constitute the HEV powertrain. These setpoints are chosen by the energy management strategy (EMS) in order to fulfil the driver's request and at the same time exploit the remaining degrees of freedom to obtain the most suitable powertrain behaviour. “Optimal” EMS that have been disclosed in these years are aimed at minimizing an objective function that typically represents the overall fuel consumption, but might include pollutant emissions, battery life degradation, under several constraints concerning battery charge, drivability, etc. In particular, charge-sustaining or autonomous HEV imply that the battery State Of Charge (SOC) at the end of a vehicle mission is required to be as close as possible to its initial value. A mathematical formulation of such a control problem has been posed in terms of optimal control [11, 12, 13, 14, 15] and numerous practical implementations for various architectures such as parallel [4, 5, 7, 16, 17, 18], series [19, 20], and combined HEV [11, 21, 22, 23] have been presented.

The class of plug-in HEV (PHEV), where the battery can be recharged

from an external source (grid) also, has attracted less research than charge-sustaining HEV, although pioneering papers have already treated this topic in terms of optimal control and presented simulation or experimental results [24, 25, 26, 27, 28]. The specific difficulty in this class of EMS is to generate an optimal discharge of the battery. Indeed it is known that a simple CD-CS strategy, i.e., a fully-electrical operation (charge depleting, CD) followed by a Charge-Sustaining (CS) operation from when the battery is discharged onwards, although attractive as it allows presenting the HEV as an “electric vehicle”, is far from being optimal from a fuel economy standpoint. Therefore, progressive battery discharge (“blended-mode”) operation is expected to be the output of an optimal EMS.

While several EMS have been generally presented in the scientific literature, a way to compare them is obviously not generally available, since studied systems and driving conditions vary from case to case. Clearly, the ability to make direct comparisons between systems, employing these algorithms, would be highly beneficial for the scientific community to verify common claims concerning both performance (optimality) and implementability (flexibility or reusability, easiness of calibration and implementation, etc.) of EMS and focus future efforts in the most promising directions. Such comparison tools have been deployed for other control applications [29] and consist of benchmark control problems that are typically solved using simulation models replacing real systems. As a second step, functional solutions might be benchmarked on physical systems as well. Recently, the Japanese automotive societies JSAC and SICE have jointly proposed a benchmark HEV control problem [30] based on a simulator of a combined hybrid (Prius-like) vehicle and driver and aimed at challenging academic researchers.

This paper presents a benchmark PHEV control problem and analyzes a set of solutions. The benchmark was developed for a special session of the IFAC Workshop on Engine and Powertrain Control, Simulation and Modeling (E-COSM ’12), held in Rueil-Malmaison, France, in October 2012. The participation of nine teams presenting their own solution demonstrated the interest in such initiative. All teams were provided with a fully functional simulator of a PHEV, and were to implement an EMS to optimize a set of criteria. The simulator (see Sect. 2) is of the quasi-static type and accounts for longitudinal vehicle dynamics and battery SOC dynamics, while the engine and electric machines are modeled using stationary maps. Solutions were to be submitted in the form of a Simulink block with a specific format (inputs/outputs/solver). The evaluation of the strategies was done on the

basis of the fuel and energy consumption for two realistic driving cycles that were unknown to the participants, as well as acceleration performance and controller runtime performance (details in Sect. 3). In the cycle tests, the battery is completely charged at the beginning of the cycle and can be depleted at the end of the cycle. The participants were able to make use of some approximated information about the cycle, namely the total distance and average speed, which could be easily retrieved from a GPS device. Given the focus of the benchmark problem, this information was included in the simulator as perfectly known, albeit in practice it is affected by measurement uncertainties. A special jury, presided by the holder of the IFP School – Fondation Tuck Chair on Hybrid vehicle and energy management, defined the two test cycles and guaranteed the correct evaluation of the solutions to be benchmarked. The nine solutions evaluated are presented in Sect. 4, while Sect. 5 discusses the results obtained. The software developed for this benchmark will be made available on the web site [www.ecosm12.org](http://www.ecosm12.org).

## 2. Simulator

Although a detailed description of vehicle propulsion systems would require the modeling of several dynamic phenomena, it has long been recognized [31] that for the purpose of fuel economy estimation, quasi-static models, i.e., based on efficiency maps measured under stationary operation of the various components, suffice to a large extent. For such a reason, quasi-static models are largely used to design and pre-assess energy management strategies of HEV, as per the literature cited within the paper. Of course, the mutual relationship between the EMS and typical transient maneuvers would not be represented by such models, but if the main focus is on the fuel economy, they can still reasonably serve to compare the global performance of different EMS. These are also the reasons why the present benchmark PHEV control problem is based on a quasi-static simulator.

The simulator provided implements a model of Chevrolet Volt, validated with published GM data, which are well reflected in the simulation results [32, 33, 35, 34]. The simulator implements three main blocks (Fig. 1): (1) Driving cycle, which computes the torque demand based on the specified driving cycle, and also outputs the preview information (nominal distance and average speed); (2) Control strategy (EMS), which was to be filled with the benchmark solutions respecting given input and output ports; (3) Vehicle and powertrain model, which contains the quasi-static model of the

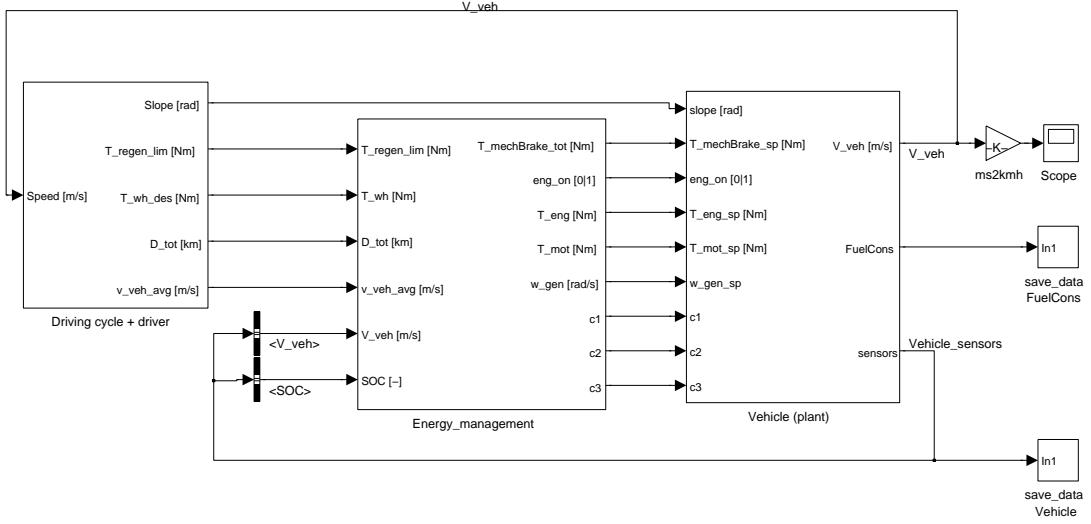


Figure 1: Benchmark simulator layout.

powertrain and vehicle dynamics.

The participants had access to the content of the driving cycle and the vehicle model block, but they were not to be modified. Only their respective outputs could be used for developing the EMS, and only the controller block was to be submitted at the end.

### 2.1. Powertrain model: GM Voltec

The powertrain architecture powering the Chevrolet Volt consists of a power-split, planetary-based system, named Voltec and shown in Fig. 2. Three clutches (C1, C2, C3) allow connecting or disconnecting the internal combustion engine (ICE), the generator (GEN) and the main traction machine (MOT). Both electric machines can actually work in both motoring and generating mode, and for both of them the sign convention is that positive torque and positive electric power indicate motoring operation.

The powertrain can operate in the following modes [32, 33, 35]:

1. One-motor EV (C1 locked, C2 open, C3 open, engine off). MOT alone propels the vehicle, powered by the battery. The planetary gear set introduces a fixed reduction between the machine MOT and rest of the driveline (final ratio and differential).
2. Two-motor EV (C1 open, C2 locked, C3 open, engine off). In this case, the machine GEN acts on the planetary ring through C2 and thus

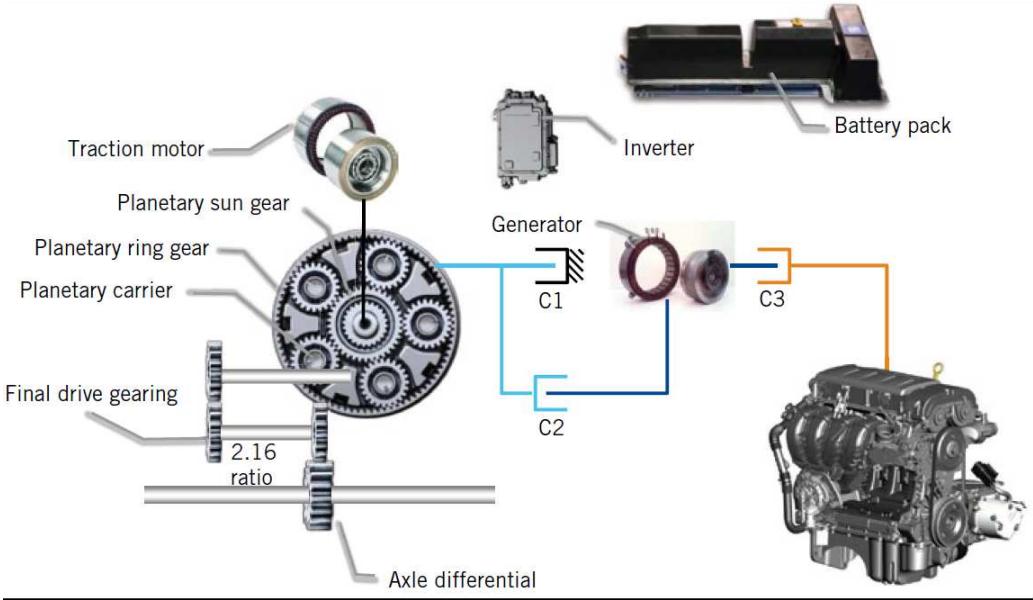


Figure 2: Kinematic architecture of GM’s Voltec [33].

it changes the gear ratio between MOT and the powertrain output. This mode is useful to reduce MOT speed at high vehicle speed, thus increasing overall powertrain efficiency by combining the use of both electric machines.

3. Range-extender mode (C1 locked, C2 open, C3 locked, engine on). This is a traditional series-HEV mode: the engine and generator are connected and produce electric power; MOT alone propels the wheels.
4. Power-split mode (C1 open, C2 locked, C3 locked, engine on). In this mode, the three machines are all connected together with a variable speed ratio that depends on the generator speed. The mode allows transmitting mechanical power directly from the engine to the wheels, thus resulting in overall higher efficiency than a pure series mode.

As a whole, the vehicle and powertrain model takes as inputs the outputs of the EMS, i.e., engine torque setpoint  $T_e$  ( $T_{\text{eng\_sp}}$  in Fig. 1), motor torque setpoint  $T_m$  ( $T_{\text{mot\_sp}}$ ), generator speed setpoint  $\omega_g$  ( $w_{\text{gen\_sp}}$ ), brake torque  $T_{br}$  ( $T_{\text{mechBrake\_sp}}$ ), engine on/off signal ( $\text{eng\_on}$ ), and clutch commands C1 to C3 ( $c_1, c_2, c_3$ ). The outputs are vehicle speed  $v$  ( $V_{\text{veh}}$ ), fuel consumption  $\dot{m}_f^*$  ( $\text{FuelCons}$ ), and the battery SOC  $\xi$  ( $\text{SOC}$ ), to be used within

the EMS.

### *Vehicle Model*

The vehicle submodel takes the wheel torque  $T_{wh}$  from the powertrain and the brake torque  $T_{br}$  command as inputs and yields the vehicle speed  $v$  and the wheel speed  $\omega_{wh}$  as output. The submodel implements vehicle's longitudinal dynamics

$$\dot{v} = \frac{r_{wh}}{J_v} [T_{wh} + T_{br} - m_v r_{wh} g \sin \alpha - r_{wh} (c_0 + c_1 v + c_2 v^2)] \quad (1)$$

where  $\alpha$  is the road slope and  $J_v$  the vehicle moment of inertia.

The relevant vehicle parameters have been extracted from [33] or estimated from similar vehicles and are listed in Table 1. All simulations are carried out by considering 97 kg in addition to the vehicle mass (75 kg driver and 35  $\ell$ , i.e., 22 kg full tank of fuel).

Table 1: Vehicle parameters

Curb weight $m_v$	1812 kg
Road law coefficient $c_0$	105.95 N
Road law coefficient $c_1$	0.01 N·s·m <sup>-1</sup>
Road law coefficient $c_2$	0.4340 N·s <sup>2</sup> ·m <sup>-2</sup>
Wheel radius $r_{wh}$	33 cm
Vehicle inertia $J_v$	207 kg·m <sup>2</sup>
Wheelbase	2685 mm
Center of gravity height	550 mm
Front/rear static weight distribution	49%/51%

### *Transmission Model*

The transmission consists of a differential gear ( $R_d = 2.16$ ), a planetary gear set (PGS), and a node (unit ratio). The generator is connected to the ring (r), the motor is connected to the sun (s) and the transmission output is the satellite carrier (c) of the PGS. The node connects the engine and the generator.

The forward transmission submodel takes the generator and wheel speeds,  $\omega_g$  and  $\omega_{wh}$ , as well as the engine and motor torques,  $T_e$  and  $T_m$  as inputs, and yields the engine and motor speeds,  $\omega_e$  and  $\omega_m$ , as well as the generator and wheel torques,  $T_g$  and  $T_{wh}$ , as outputs.

The kinematic relation between the speeds of three elements of the planetary gear set is

$$\rho \cdot \omega_r + \omega_s = \omega_c \cdot (\rho + 1), \quad (2)$$

where  $\rho$  is the ratio between the number of teeth of the ring and the sun gear:  $\rho = N_r/N_s = 83/37 = 2.24$ . The torque relations imposed by the planetary gear set are

$$\frac{T_r}{\rho} = \frac{T_c}{\rho + 1} = T_s \quad (3)$$

The connection between PGS elements and power converters depends on the mode in which the powertrain is operated. See Table 2 for mode-dependent correspondances.

Table 2

Mode 1	$\omega_r = 0$ $T_g = 0$	$\omega_e = 0$
Mode 2	$\omega_r = \omega_g$ $T_g = \rho \cdot T_m$	$\omega_e = 0$
Mode 3	$\omega_r = 0,$ $T_g = -T_e$	$\omega_e = \omega_g$
Mode 4	$\omega_r = \omega_g$ $T_g = \rho \cdot T_m - T_e$	$\omega_e = \omega_g$
All Modes	$\omega_m = \omega_s,$ $T_m = T_s,$	$\omega_c = R_d \cdot \omega_{wh}$ $T_{wh} = R_d \cdot T_c$

The simulator is implemented using these relations, including the gear efficiencies but neglecting the dynamics of the machines and the inertia of the gears.

### Engine Model

The engine submodel takes  $\omega_e$  and  $T_e$  as inputs and yields the fuel consumption  $\dot{m}_f^*$ . Since a quasi-static modelling approach is used, the engine is represented by its fuel maps, shown in Fig. 3. Torque and speed limits are enforced. Special treatments are used to represent cranking and idle phases. When the engine is switched on, the model generates a predefined negative torque (-25 Nm) for a short period (1 s), after which the torque generated matches the setpoint.

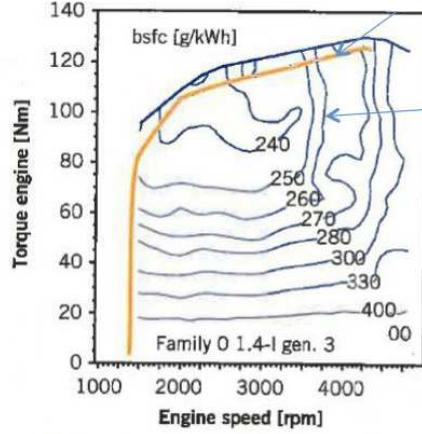


Figure 3: Engine fuel map [33].

### *Motor and Generator Model*

The motor submodel takes the motor torque  $T_m$  and speed  $\omega_m$  as inputs and yields the electric power  $P_m$  as output. Similarly for the generator submodel  $T_g$  and  $\omega_g$  are the inputs and  $P_g$  is the output. The electric machines are represented by their efficiency maps, which are shown in Fig. 4. Torque and power limits are enforced. The generator model also enforces a maximum rate of change of  $\omega_g$  ( $200 \text{ rad/s}^2$ ) to represent machine inertia.

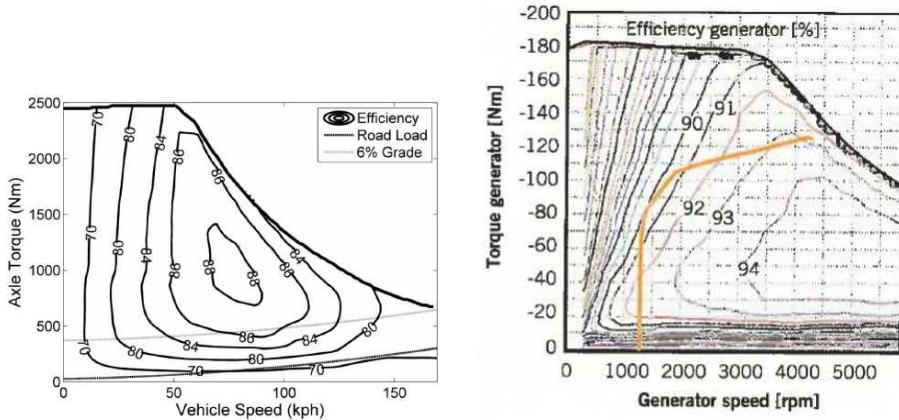


Figure 4: Combined motor-transmission efficiency map (top) [34] and generator efficiency map (bottom) [33].

### Battery Model

The battery submodel takes the overall electrical power  $P_b = P_g + P_m$  and the current SOC as input and yields the SOC at next time step as well as the inner or electrochemical battery power  $P_{ech}$ . The model is based on a simple equivalent circuit composed of a voltage source  $V_{oc}$  and a resistance  $R_b$  in series, both functions of the SOC ( $I_b$  is the battery current),

$$P_{ech} = V_{oc}I_b, \quad I_b = \frac{V_{oc}}{2R_b} - \sqrt{\frac{V_{oc}^2 - 4R_bP_b}{4R_b^2}} \quad (4)$$

$$\dot{\xi} = -\frac{I_b}{Q_b} \quad (5)$$

where  $Q_b$  is the charge capacity. Power, current, and voltage limits are enforced. Moreover, SOC operation within a prescribed window is enforced.

In the case of the Volt, only the basic battery parameters, collected in Table 3, are published. For the lack of specific data, the internal resistance and the open circuit voltage characteristic of a single Li-ion cell are assumed to be the same as the experimental data in [36].

Table 3: Battery parameters

parameter	value	source
Total energy capacity	16 kWh	[33]
Total nominal voltage	360 V	[33]
SOC range	65%	[33]
Number of cells in series	96	[35]
Number of strings in parallel	3	[35]
Peak current	400 A	[35]
Peak power (charge)	110 kW	
Peak power (discharge)	-60 kW	

### 2.2. Driver model

The driver model is responsible for yielding the powertrain torque request  $T_d$  (`T_wh_des` in Fig. 1) to the EMS as a function of the vehicle speed  $v$  (`V_veh`) measured from the vehicle model output. For the two cycle tests, the model is a cascade of (i) a feedforward calculation of the torque request

as a function of the desired speed  $v$ , and (ii) a PI regulator as a function of the difference between cycle speed and  $v$ . The term (i) is calculated as

$$T_d = \begin{cases} T_{d,tot}, & T_{d,tot} \geq 0, \\ (1 - \sigma)T_{d,tot} - \frac{T_{d,tot}H_{CG}}{m_v g r_{wh} B_w}, & T_{d,tot} < 0 \end{cases} \quad (6)$$

$$T_{d,tot} = \frac{\dot{v} J_v}{r_{wh}} + r_{wh} (c_0 + c_1 v + c_2 v^2 + m_v g \sin \alpha) \quad (7)$$

where the wheel torque request  $T_{d,tot}$  is obtained from the inversion of (1),  $H_{CG}$  is the height of the center of gravity,  $B_w$  the wheelbase, and  $\sigma$  the static weight distribution (see Table 1). The proportional and integral gains of the term (ii) are tuned as  $K_P = 500 \text{ N}\cdot\text{s}$ ,  $K_I = 1 \text{ N}$ .

For acceleration tests, only the PI regulator is used, with a reference speed set to a very high value in order to enforce full torque demand. The test end is detected as a function of the speed or the distance covered, according to the particular test. Conversely, the braking test is split into two parts, with a first part to reach 100 km/h through a PI regulator, then a second part with constant negative torque request.

### 2.3. EMS

The EMS block to be filled by benchmark participants takes as inputs the driver torque demand  $T_d$  output by the driver's model (`T_wh` in Fig. 1) and the vehicle speed  $v$  (`V_veh`) and the SOC  $\xi$  (`SOC`) yielded by the vehicle and powertrain model. The expected outputs of the EMS model are the engine and motor torque setpoints, the generator speed setpoint, the clutch commands, the engine on/off state, and the mechanical brake torque, all sent to the vehicle and powertrain model.

## 3. Benchmarking

### 3.1. Scoring metrics

Each solution has been evaluated according to several metrics, listed in Table 4. The overall score is obtained by weighting each metric by the factor shown in the table. The weights are intended to be a compromise between energy efficiency (50%) and expectations of manufacturers (20%) and end users (30%). Since they intervene only in the final evaluation stage of the benchmark, they can be easily modified in future versions of the benchmark to reflect a different focus. Although a correlation is expected between energy

efficiency sub-metrics, they are accounted for separately in order to emphasize the effects of residual battery energy and the CO<sub>2</sub> factor. The actual scoring is obtained by normalizing the result obtained in each metric with respect to the average value for that metric calculated over all valid solutions. Note that all scores are best when minimized.

Table 4: Scoring metrics

	Metric	Weight
Performance (30%)	Acceleration 0–100 km/h [s]	7.5%
	Acceleration 70–120 km/h [s]	7.5%
	Acceleration 0–1000 m on 4% slope [s]	7.5%
	Braking distance from 1000 km/h [m]	7.5%
Energy and economy (50%)	Total energy use (fuel+electricity) [MJ]	15%
	Fuel consumption [MJ]	20%
	Tailpipe emissions (not modeled)	0%
	Well-to-wheel CO <sub>2</sub> emissions [kg]	15%
Computational performance (20%)	Processor use [s]	10%
	Memory use [kB]	10%

### *Performance*

Four performance tests are enforced in the driver’s model, see Sect. 2.2. Elapsed simulation time or distance covered until the simulation stop are monitored and used as metrics.

### *Energy and economy*

These metrics are the sum of the results in two different driving cycles, based on real-world data, whose length (see Sect. 3.2) exceeds the all-electric range of the vehicle. In each cycle, the initial SOC must match the value given in the data file provided with the simulator, while the final SOC must be at least equal to a target final value. CO<sub>2</sub> emissions were calculated from energy use results as the total emissions from fuel combustion, fuel production (well-to-tank), and electricity production. For electricity, Europe average emissions were to be taken into account (data for France, US, and China were also provided for information). The coefficients in Table 5 were used to compute the CO<sub>2</sub> emissions. Tailpipe emissions were not considered for simplicity (unavailable reliable modeling) and due to their weak dependency on the EMS for warm engine conditions.

Table 5: Data for CO<sub>2</sub> emissions

Gasoline well-to-tank emissions [37]	12.5 gCO <sub>2</sub> /MJ of fuel
Gasoline combustion [37]	73.4 gCO <sub>2</sub> /MJ of fuel
Electricity production (emissions for electricity and heat production [38], average 2007–2009)	Europe average: 94.7 gCO <sub>2</sub> /MJ France: 24.7 gCO <sub>2</sub> /MJ US: 147.5 gCO <sub>2</sub> /MJ China: 207.8 gCO <sub>2</sub> /MJ World average: 140 gCO <sub>2</sub> /MJ

### *Computational Performance*

Processor use and memory use were monitored on the computer running the simulation. The former was evaluated using MATLAB functions `tic` and `toc` before and after each test, the latter using MATLAB function `sldiagnostics`. Only for fuel economy tests, the actual results are averaged over four runs, in order to reduce the effects of other possible instances running on the test computer. Counting of floating point operations could be used to make these metrics less dependent on the particular machine. However, albeit an option for future versions of the benchmark, this solution has not implemented due to the lack of a simple flop counting function in the most recent versions of MATLAB.

### *Solution validity*

At all times, all component limitations detailed in the data file (max/min power, torque, state of charge, speed etc.) were to be respected in all components; failure to do so during any simulation invalidated the corresponding results.

### *3.2. Driving cycles*

Driving cycles were defined by the benchmark jury as “surprise” cycles, not communicated in advance to the participants. The two real-life cycles selected are shown in Figs. 5–6. The first cycle is actually the combination of two trips recorded in the German city of Aachen, namely, an urban trip spanning 16.2 km and a mixed-drive trip spanning 28.4 km. Elevation has been set to zero for the whole cycle. In order to allow full battery depletion if the HEV would be operated in EV modes, the combined Aachen cycle is repeated three times.

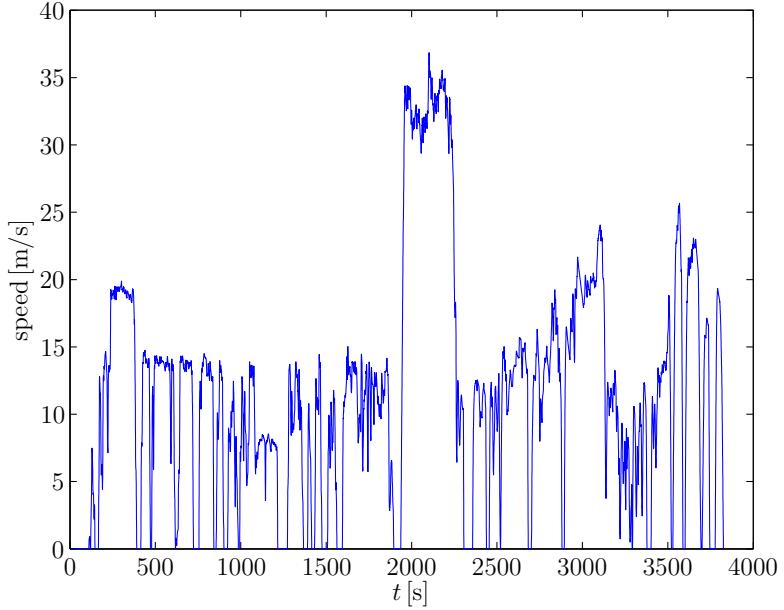


Figure 5: Aachen cycle.

The second cycle is a trip recorded between Arco and Merano, Italy (in the Alps), spanning 157.7 km and including severe altitude variations that are visible in Fig. 6.

A summary of cycle statistics is listed in Table 6.

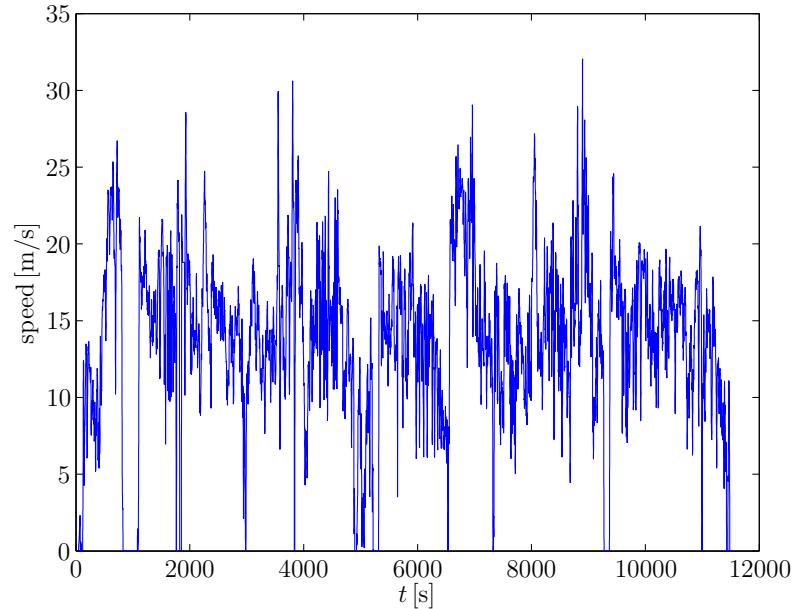
## 4. Proposed Solutions

### 4.1. Introduction

The benchmark control problem can be summarized as to find a control policy  $u(t)$  for  $t = 0, \dots, T$  where  $T$  is any test duration, in such a way to minimize the score defined in Sect. 3. For each single metrics, this is equivalent to minimize a cost function  $J(u)$ , where the control vector  $u \triangleq \{T_e, T_m, \omega_g, C_1, C_2, C_3, B_e, T_{br}\}$  defines the powertrain mode and the operating point of each component. In the example of the total energy use metrics,

$$J = LHV \cdot \int_0^T \dot{m}_f^*(u, w) dt + \int_0^T P_{ech}(u, w) dt \quad (8)$$

(a)



(b)

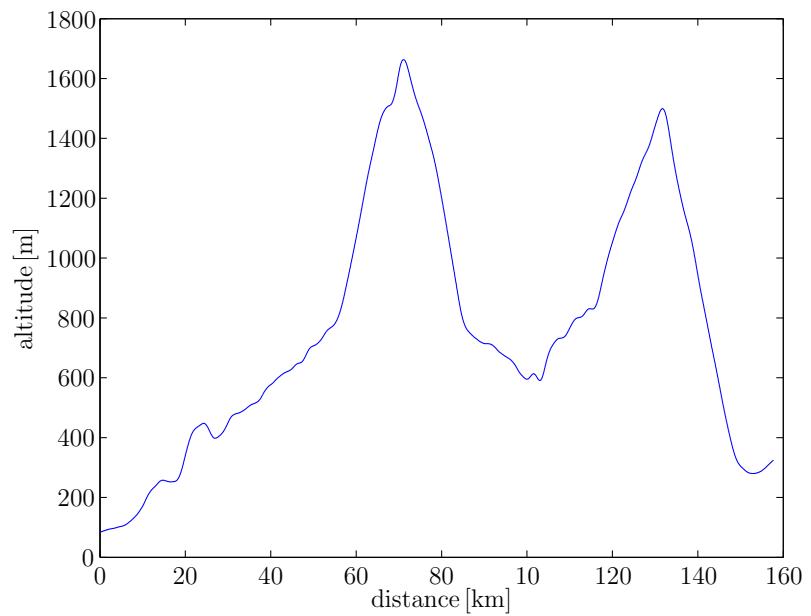


Figure 6: Arco to Merano cycle, (a) speed profile, (b) altitude profile.

Table 6: Cycle statistics. Notes: a) the actual test cycle consists of three repetitions of Aachen urban cascaded by Aachen mixed.

	Aachen urban <sup>a</sup>	Aachen mixed <sup>a</sup>	Arco–Merano
Length [km]	16.2	28.4	157.7
Max speed [km/h]	71.6	132.6	115.4
Average speed [km/h]	30.3	53.8	49.2
Duration [s]	1926	1871	11549
Max acceleration [m/s <sup>2</sup> ]	3.9	4.7	5.7
Max deceleration [m/s <sup>2</sup> ]	3.0	4.6	7.4
No. of vehicle stops	14	11	15
Total stop time [s]	430	185.5	671.5
Total stop time [%]	22	10	6
Altitude variation [m]	0	0	1579

where the disturbance vector  $w(t) \triangleq \{v(t), T_d(t)\}$  comprises the exogenous inputs (not known in advance) and  $LHV$  is the lower heating value of the fuel. The minimization (8) is subject to the SOC constraint,  $\xi(T) \geq \xi_{min}$ , and other constraints. Formulated as such, the benchmark control problem is formally equivalent to a constrained optimal control problem.

Data published by GM [33] show that, in the Volt embodied strategy, mode selection depends primarily on SOC status. For charge-depleting (CD) operation (high SOC), modes 1 or 2 are selected according to vehicle speed and required torque, see Fig. 7. When the SOC becomes low, charge-sustaining operation (CS) is activated, which consists of three modes 1, 3, and 4, again selected as a function of vehicles speed and desired torque. This SOC-regulating policy depends on the fact that the Volt is classified as a range-extended electric vehicle. In the benchmark control problem, participants were allowed to activate a “blended-mode” (BM) strategy to regulate the SOC, i.e., to start the engine before the SOC reaches a lower-end value. Of course, battery-recharge (BR) operation aimed at restoring the battery charge to a certain value was possible as well.

Nine control solutions were submitted to the benchmark problem. Table 7 summarizes the approaches implemented in the proposed solutions. The column “EMS technique” classifies the entries according to the type of control design. Two approaches are represented, namely, based on rules (heuristic) or based on optimal control theory and particularly on the Pontryagin Minimum

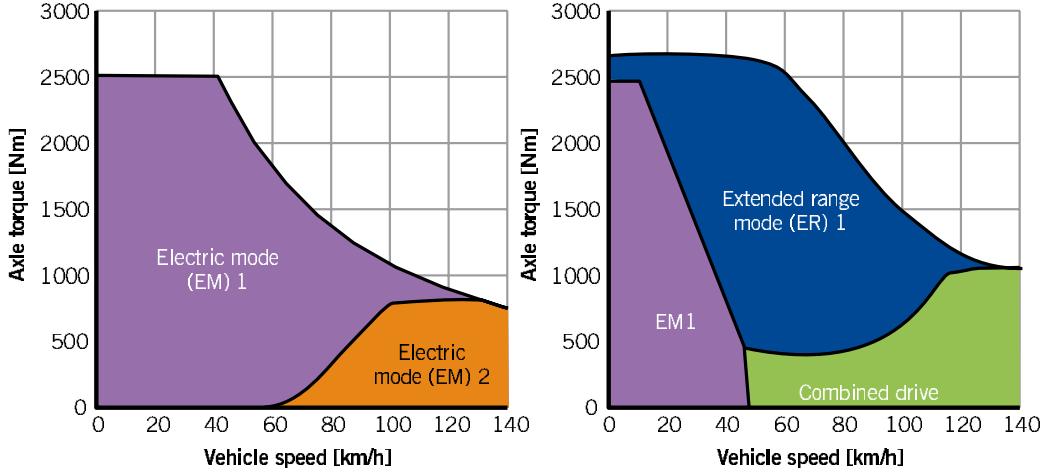


Figure 7: Operating modes of GM's Voltec as a function of vehicle speed and desired torque [33].

Principle (PMP). Additionally, the table classifies the nine solution according to the discharge strategy, the mode selection strategy, and the operating point selection strategy.

All the used techniques are further illustrated below. More details on two solutions are provided in the ECOSM'12 papers [39, 40].

Table 7: List of solutions to the PHEV control benchmark. Notes: a) with 10% driving distance underestimation; b) enhanced with exception rules; c) adaptive ECMS with varying SOC reference

Solution	EMS technique	Discharge strategy	Mode selection	Operating point selection
S1	ECMS	BM <sup>a,c</sup>	Map based	Map based
S2	Heuristic	CD-CS	Map based <sup>b</sup>	Map based
S3	ECMS	BM <sup>c</sup>	Vector based	Vector based
S4	Heuristic	BM	Rule based	Rule based
S5	Heuristic	BM	Rule based	Rule based
S6	Heuristic	BM	Rule based	Map based
S7	ECMS	BM <sup>c</sup>	Vector based	Vector based
S8	ECMS	BM <sup>c</sup>	Vector based	Vector based
S9	Mixed	?	Rule based	Rule based

#### *4.2. Heuristic controllers*

Heuristic EMS are based on intuitive rules and correlations involving various vehicular variables. One guiding principle is to use the engine when its efficiency can be relatively high, while in less favorable conditions the electric modes should be given preference and the engine should be turned off. Moreover, when the engine is on, it should be operated in the highest possible efficiency regions (i.e., at high loads). Two common approaches to implement these intuitive principles are the map-based and the rule-based approach. In the map-based approach, the output setpoints are stored in multi-dimensional maps whose entries are measured quantities describing the state of the powertrain. In the rule-based approach, the EMS is either coded as a set of logic rules or implemented as a finite state machine (FSM).

In most solutions (S2, S4, S6, and S9), a two-level architecture is implemented. A high-level supervisor (see Fig. 8a) first selects the powertrain mode and the engine power setpoint  $P_e$ . The former output is either mapped (S2) as a function of  $v$ ,  $T_t$ , and  $\xi$  and enhanced with exception rules, or calculated by a finite-state machine (S4, S9) with transition rules as a function of the same vehicular quantities. Engine power is calculated from rules as a function of the same variables and of the distance  $D_t$ , either in order to implement a CD–CS SOC-regulation strategy (S2) or a blended-mode strategy (S4) by minimizing a performance criterion.

The cascaded low-level controller evaluates the engine, motor, and generator setpoints, as well as the clutch commands, according to the mode selected and the engine power. While for mode 1 there is no degree of freedom, other modes require additional choices. Optimal operating point map of the engine is used to calculate  $T_e$  and  $\omega_e$  as a function of  $P_e$ , while the other setpoints are such to fulfill transmission kinematics/dynamics. In S9 (a mixed-approach strategy) this task is performed using ECMS (see Sect. 4.3) for mode 4.

An alternative control architecture (used in S6, Fig. 8b) is such that the high-level supervisor selects CD operation or BR operation as a function of  $\xi$ ,  $T_t$ ,  $v$  and the information on the distance-to-go. In the case of CD operation, the low-level controller selects mode 1 or mode 2 by minimizing the electric consumption and determines electric setpoints. In the case of BR operation, the low-level controller operates the engine either to maximize the recharge efficiency or the recharge power and selects accordingly the setpoints using predefined maps.

A simpler approach (used in S5) switches between electric modes and engine-on modes as a function of the difference between  $\xi$  and a reference SOC profile based on the distance-to-go. If on, the engine is operated at its best-efficiency point and mode 4 is actuated, with exceptions possibly shifting the engine operating point or enforcing mode 3.

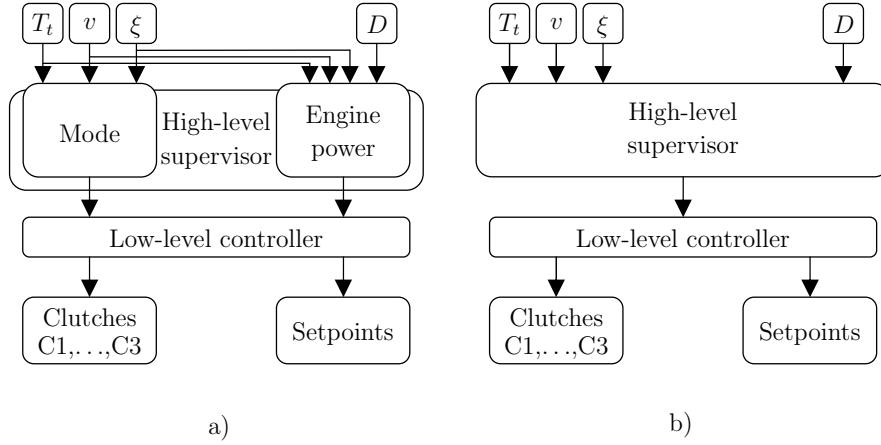


Figure 8: General heuristic strategy flowchart (a) and variant (b).

#### 4.3. ECMS

The second approach used in the proposed solution is that based on optimal control. Since early 2000's it has been shown that the control problem of minimizing the fuel consumption of a HEV over a driving mission, while letting its SOC tend to a target value  $\xi_{ref}$  can be formulated as an optimal control problem similar to (8). Offline solutions to such a problem, that is, solutions that make use of the prior knowledge of the driving profile can be calculated using dynamic programming or directly solving the Euler-Lagrange formulation of optimal control. In the latter case, the optimal control policy is found as

$$u^o(t) = \arg \min_u H(u, w(t), \xi(t)) = \arg \min_u LHV \cdot \dot{m}_f^*(u, w(t)) + \lambda(t) \frac{d\xi(t)}{dt} \quad (9)$$

under the state and costate dynamics

$$\frac{d\xi(t)}{dt} = -\frac{I_b(u, w, \xi)}{Q_b}, \quad \frac{d\lambda(t)}{dt} = -\frac{\partial H(u, w, \xi)}{\partial \xi}. \quad (10)$$

Under the approximation  $\partial V_{oc}/\partial \xi \approx 0$ ,  $\partial R_b/\partial \xi \approx 0$ ,  $\lambda$  is a constant and the strategy (9) reduces to offline technique commonly known as Equivalent Consumption Minimization Startegy (ECMS)

$$u^o(t) = \arg \min_u LHV \cdot \hat{m}_f(u, w(t)) + s^o P_{ech}(u, w(t)) \quad (11)$$

with the equivalence factor defined as  $s^o = -\lambda/(V_{oc}Q_b)$ . The value  $s^o$  fulfills the global constraint on SOC, i.e.,  $\xi(T) = \xi_{ref}$ .

#### 4.3.1. Costate adaptation

While in offline ECMS  $s^o$  can be calculated using iterative root-finding algorithms, in online application it has to be continuously adapted and thus a variable  $s(t)$  replaces  $s^o$  in (11). The most common approach for such adaptation, which proves to be directly related to Hamilton-Jacobi-Bellman optimal feedback control [12], is a feedback on current SOC:

$$s(t) = s_0 - k_p(\xi(t) - \xi_{ref}) - \dots, \quad (12)$$

where the ellipsis indicates possible integral or nonlinear terms.

All solutions (S1, S3, S7, S8, and S9 when ECMS is used) include in the right-hand side of (12) a term proportional to the integral of the error  $\xi(t) - \xi_{ref}$ . However, S8 uses a modified coding where  $s$  is initialized to a value  $s_0$ , updated according to a space-depending version of (12) when a prefixed sampling distance is covered, and reset to  $s_0$  at each time the reference SOC is tracked back [41]. A nonlinear term in the form of a tangent-like function of the error is added to the proportional-integral terms in S1 [40]. The feedforward term  $s_0$  is variously calculated as a function of the average speed and the distance (S1, S8), the average speed only (S3), or it is constant (S7).

While  $\xi_{ref}$  clearly equals the initial value of SOC,  $\xi(0)$ , for CS operation, plug-in hybrids allow for discharging the battery and thus a different definition for  $\xi_{ref}$  must be used. Recent literature has addressed this problem and the most common strategy is to use a varying, i.e., decreasing  $\xi_{ref}(t)$  aimed at implementing a BM operation. The decrease of  $\xi_{ref}$  should represent the advance in the mission and toward its end,  $\xi_{ref}(T)$  should tend to  $\xi_{min}$ . All five solutions (S1, S3, S7, S8, and S9) adopt a linear variation of  $\xi_{ref}$  with the distance covered  $D(t)$ , namely,

$$\xi_{ref}(t) = \xi(0) - k_\xi \frac{D(t)}{D_{tot}}, \quad k_\xi = \xi(0) - \xi_{min}. \quad (13)$$

This approach clearly require the prior estimation of the distance to be covered  $D_{tot}$ .

#### 4.3.2. ECMS Implementation

The vectorial implementation of strategy (11), used in S3, S6, and S8, requires discretizing the field of admissible values  $u(t) \in \{u_q(t)\}$ ,  $q = 1, \dots, N$  at any time step. Thus,

$$\begin{aligned} u^o(t) &= u_{q^o(t)}(t), \quad \text{where} \\ q^o(t) &= \arg \min_q H_q(t), \quad \text{and} \\ H_q(t) &= LHV \cdot \overset{*}{m}_f(u_q(t), w(t)) + s(t) \cdot P_{ech}(u_q(t), w(t)). \end{aligned} \tag{14}$$

The vector size  $N$  and the nature of  $u$  varies from solution to solution. For each  $q$ ,  $u_q$  is obtained by imposing a set of predefined values to independent components of  $u$  (degrees of freedom, DoF) and calculating the dependent components through kinematic and other physical constraints. The powertrain mode is clearly a DoF itself, thus  $N = \sum_{i=1}^4 N_i$ . In mode 1 there is no additional degree of freedom and thus  $N_1 = 1$ . In mode 2 there is one speed DoF (either  $\omega_m$  or  $\omega_g$ ). In mode 3 the DoF is engine power  $P_e$  since engine speed and torque are obtained by maximizing the engine-generator efficiency for a given power. In mode 4 there are one speed and one torque independent DoFs. As an example, S8 uses  $N_{\{2,3,4\}} = 21$ .

From (14), it is clear that  $q^o(t)$  and thus  $u^o(t)$  depend only on  $w(t)$  and  $s(t)$ . Since  $w(t)$  is a two-dimensional vector (speed and torque at the wheels), the energy management output is completely determined by three variables. While the dependency of the Hamiltonians  $H_q(t)$  on SOC is neglected in the ECMS,  $s(t)$  does depend on  $\xi(t)$ , as well as on the distance  $D(t)$ . This fact suggests decoupling the evaluation of the energy management output in a two-step process, where first  $s(t)$  is evaluated using (12) and subsequently  $u^o(t)$  is evaluated as

$$u^o(t) = F_U(w(t), s(t)) \tag{15}$$

where  $F_U(w, s)$  is a look-up table where the offline-calculated results of (14) are stored. The advantage of this map-based implementation, used in S1, in terms of computing time with respect to the vectorial implementation, i.e., the online solution of (14) is evident. Moreover, the map-based implementation can be generated off line using a much finer discretization (i.e., a much higher  $N$ ) than its vectorial counterpart. S1 uses a total of 7 maps [40].

#### 4.4. Implementation issues

Since CPU use and memory use are among the scoring metrics, all solutions pay a particular attention in trying to reduce them.

Concerning the heuristic solutions, implementation of rules reduces memory use, while use of maps reduces CPU time consumption. Other techniques adopted include:

- simplification of look-up tables (S2),
- disabling of inactive Simulink subsystems, triggered subfunctions (S1, S2, S6),
- only native Simulink blocks without maps (S5),
- reduction of complexity for modes 2 and 3 (S9).

Concerning ECMS-based solutions, vector-based implementation reduces memory use while map-based implementation reduces CPU time consumption. Other techniques adopted include:

- iterative sparsification of maps (S1),
- use of Matlab S-functions (S3),
- setpoint candidate reduction (S3),
- use of vector merging instead of multi-dimensional matrices for setpoint candidates (S7).

Enforcing component limits is a delicate issue that has a strong impact on the solution validity (see Sect. 3.1). Two main approaches have been followed in the proposed solutions:

1. A priori limitation (S3, S6, S7), where map inputs or ECMS degrees of freedom are preliminarily saturated to corresponding limits: in this approach actual limits might take into account also limits induced by the concurrent operation of other components; for example, the engine torque could be constrained by the generator limits at the corresponding speed and such a method often introduces iterations, algebraic loops that deserve a special treatment (S7).
2. A posteriori limitation (S2, S5), where map outputs or ECMS candidates are checked and possibly saturated to their respective limits.

A combined approach, with a priori and a posteriori check, is used in S1, S8, and S9.

## 5. Results

### 5.1. Proposed Solutions

Table 8 summarizes the main scores obtained by running the proposed solutions.

Table 8: Benchmark results. Fuel A: cycle Arco–Merano; Fuel B: cycle Aachen; Notes: a) test disqualified due to constraints not met, result set to maximum valid if lower; b) test invalid, cycle not entirely driven; c) entry or test not considered for average calculation.

Solution	Fuel A L/hkm	Fuel B L/hkm	Memory kB	Proc. time 100 = Avg.	Score
S1	2.86	1.83	153	16	0.836
S2	3.18	2.27	81	14	0.850
S3	3.56	1.86	24	84	0.877
S4	3.39	2.57	159	18	0.934
S5	3.66 <sup>a,c</sup>	4.60 <sup>a,c</sup>	36	13	0.993
S6	3.66	4.60	186	18	1.086
S7	3.05	1.88	298	197	1.119
S8	6.06 <sup>a,c</sup>	4.99 <sup>a,c</sup>	353	442	1.873
S9 <sup>c</sup>	NA <sup>b</sup>	8.93	95	361	NA

A comparison between all valid solutions in terms of SOC trajectory for cycle “Arco–Merano” is shown in Fig. 9. The figure clearly shows that best performing strategies, i.e., S1 and S7 (see respective scores in Table 8), are able to drive the SOC toward the minimum value before the last downhill in a smooth fashion. In contrast, solutions S3 and S5 suffer from SOC oscillations around the best-performing trajectory, solutions S2 and S4 tend to discharge the battery too fast, while S6 and S8 are characterized by heavy SOC deviations with respect to the best-performing trajectory. In the following section, the best-performing strategy S1 is detailed and compared with the optimal solution of Problem 8 calculated using an offline PMP algorithm.

Two among the three best performing solutions (S1 and S3) have adopted ECMS, alongside with two other solutions (S7, which is among the best performing strategies in the fuel economy tests, and S8). It is apparent that the performance of ECMS strongly depends on the implementation of (12). All four solutions have adopted (13) with possible SOC margins. As a consequence, the  $\xi_{ref}(t)$  signal is decreasing almost linearly with the increase of time and distance covered, as shown in Fig. 10.

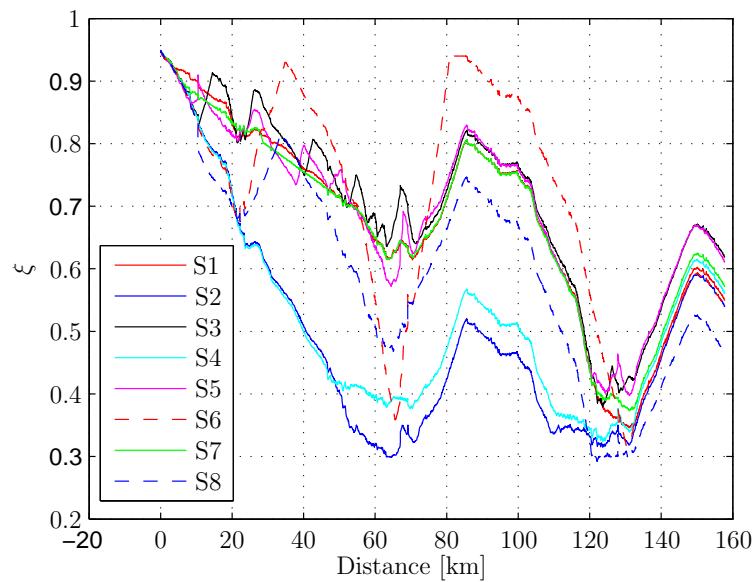


Figure 9: Cycle Arco–Merano, SOC for all valid strategies.

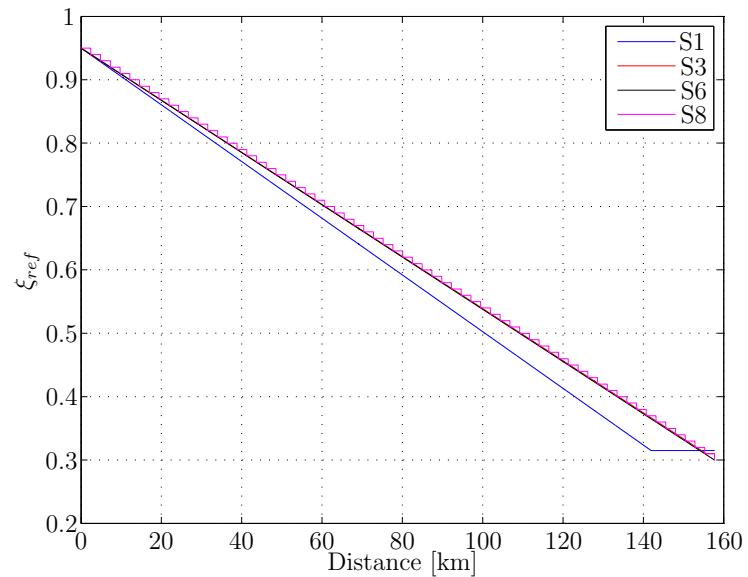


Figure 10: Cycle Arco–Merano, reference SOC for all four ECMS strategies.

Table 8 shows a weak correlation between fuel economy results and memory use, resp., processing time results. Discrepancies are particularly visible for solutions S7 and S5. The latter is the simplest solution, so it performs rather well both in terms of CPU time and memory use. On the other hand, S7 has the second-best aggregate score in the fuel economy tests but it is penalized in terms of CPU time by the use of long ECMS-candidate vectors and in memory use by the use of large maps. Generally speaking, ECMS-based strategies require Hamiltonian minimization and thus need a larger CPU time than heuristic strategies; however S1 that is map-based rather than vector-based performs better than S3, S7, and S8 in terms of CPU time. As for memory use, there is no clear trend among ECMS and heuristic strategies, since both require maps and look-up tables either to represent the various components' efficiency, or to store the pre-calculated setpoints or rules.

The final scores shown in Table 8 were calculated using the European CO<sub>2</sub> emission factor, as explained in Sect. 3.1. If other CO<sub>2</sub> factors were used, the scores would change only slightly and the ranking of the proposed solutions would remain the same. A different focus in weighting the scoring metrics would obviously lead to a different ranking. For instance, an enhanced focus on computational performance (raised from 20% to 40%) would let S2 have a better overall score than S1. On the other hand, an enhanced focus on energy efficiency (raised from 50% to 75%) would confirm S1 as the best solution. Since performance metrics are similar for all solutions, enhancing their weight (e.g., raising it from 30% to 65%) would not change the ranking at all. However, setting different weights would have probably led to differently focused solutions, so that the previous discussion must be taken very cautiously.

### *5.2. Globally Optimal Solution*

To assess the optimality of the best-performing strategy S1, it has been compared with the outcome of an offline optimization tool (HOT, [42]) that has prior knowledge of the driving cycle. HOT is based on PMP and finds iteratively the initial values of the costates. Model parameters are the same as in the Voltec simulator. The optimization criterion set is fuel consumption. Although having the capability of running cold-start cycles and performing two- or three-state optimization with engine and aftertreatment temperatures as additional state variables ([43]), for this test the standard functionality with SOC as the single state has been used. The constant value of the

equivalence factor  $s_0$  is found with a root-finding algorithm based on the SOC at the end of the test cycle,  $\xi(T)$ . The target value for the SOC is set to  $\xi_t = 30\%$ : positive deviations  $\xi(T) - \xi_t$  make  $s_0$  decrease in the next iteration, while negative deviations make  $s_0$  increase.

Figure 11 compares the optimal profiles of SOC and fuel consumption calculated by HOT for test cycle “Aachen” with the outcome of S1. The two profiles are very close to each other. Wider differences are visible in Fig. 12 that refers to the test cycle “Arco–Merano”. However, in this case too, S1 is able to make the SOC approach the minimum value (30%) before the final downhill, at the end of which both S1 and HOT predict a SOC of about 50%. Consequently, the fuel consumption predicted by S1 is very close to the minimum value calculated by HOT (2.76 l/hkm for test cycle “Arco–Merano”, 1.77 l/hkm for test cycle “Aachen”), see Table 8.

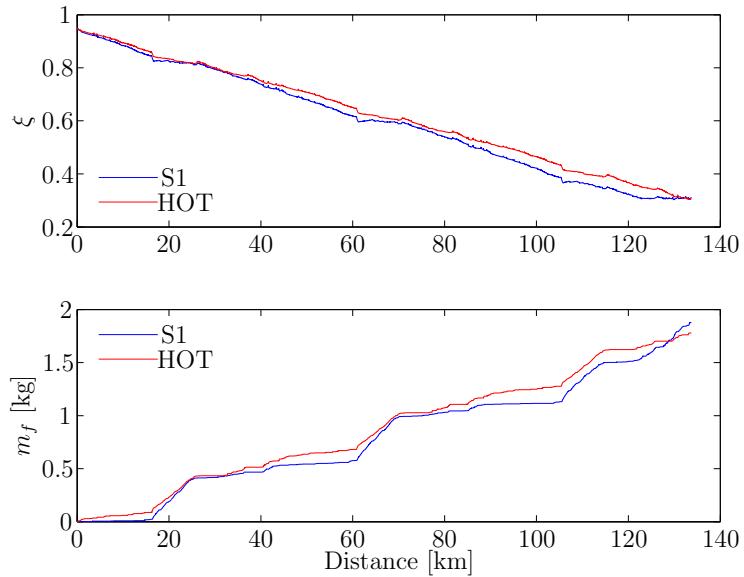


Figure 11: Aachen cycle, SOC and fuel consumption.

Figures 13–14 show the distribution of engine operating points during the two test cycles. Both S1 and HOT tend to operate the engine around the best efficiency region, although S1, being an online strategy, is characterized by many more distinct operating points (transient maneuvers, SOC regulation, etc.) than HOT. Figures 15–16 compare the two distributions of powertrain

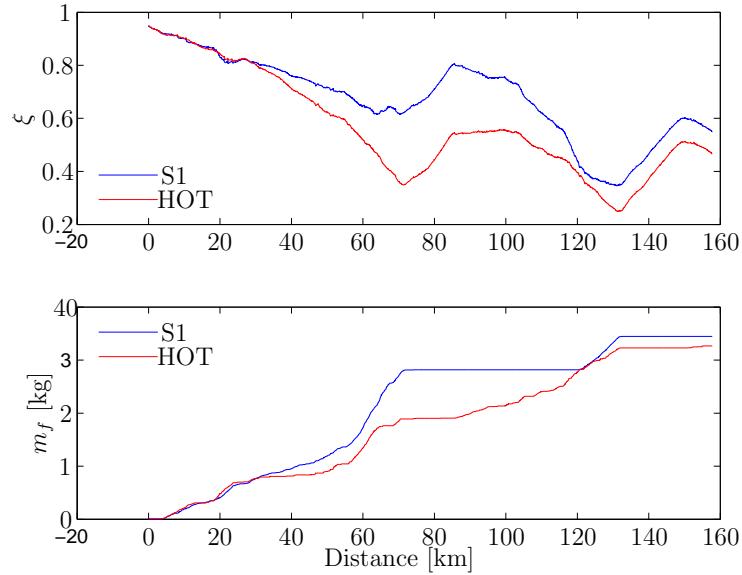


Figure 12: Arco–Merano cycle, SOC and fuel consumption.

modes as a function of vehicle speed and torque. In both strategies, mode 1 is selected at low speeds, mode 2 for medium speeds and low torques, mode 3 at high torques, and mode 4 for medium to high speeds. The S1 use of the mode 3 is wider than in HOT, certainly in the attempt of perform a blended-mode strategy as a function of SOC. The behavior in the two cycles is similar for both strategies, except for the different speed and torque range.

## 6. Conclusions

The development of benchmark control problems is an engineering practice that can help assessing different methods and techniques under the same circumstances (same system, same operating conditions, same exogenous inputs, etc.). The benchmark control problem illustrated in the paper, concerning the energy management of a plug-in hybrid-electric car, has fulfilled this goal since it has allowed:

1. a comparison in terms of various performance criteria: while the dispersion among different solutions in terms of vehicle performance is rather low, fuel economy is more sensitive to the energy management

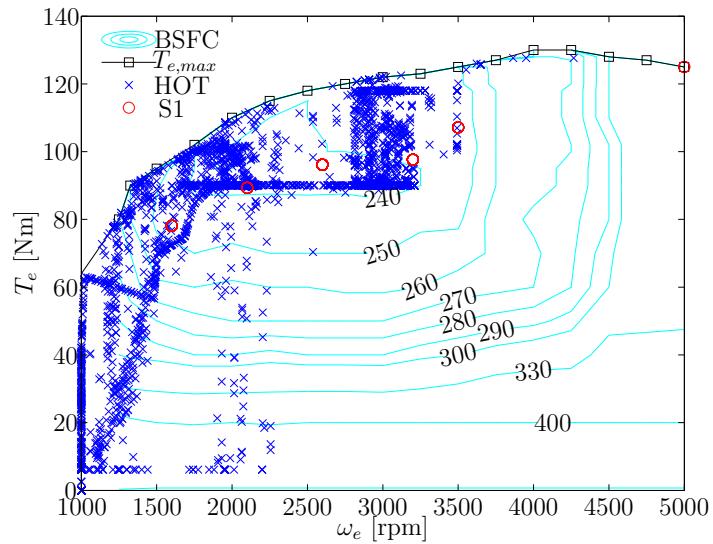


Figure 13: Aachen cycle, engine operating points.

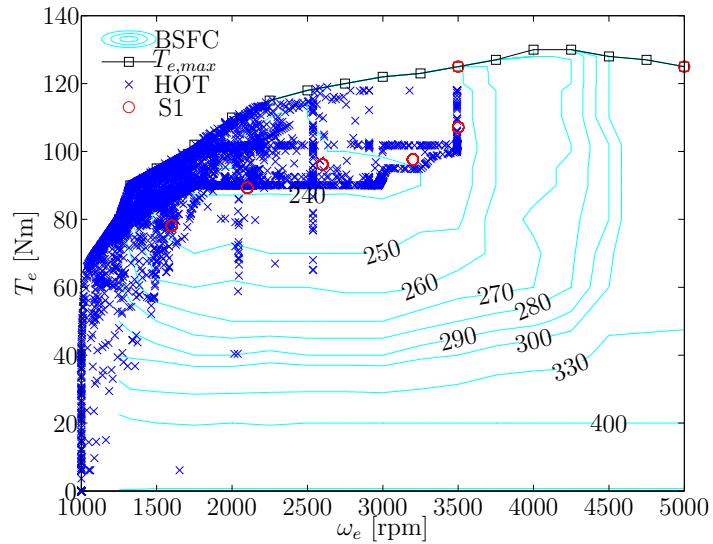


Figure 14: Arco-Merano cycle, engine operating points.

strategy adopted, particularly for real-life driving profiles with severe altitude variations; even larger differences can arise in terms CPU time

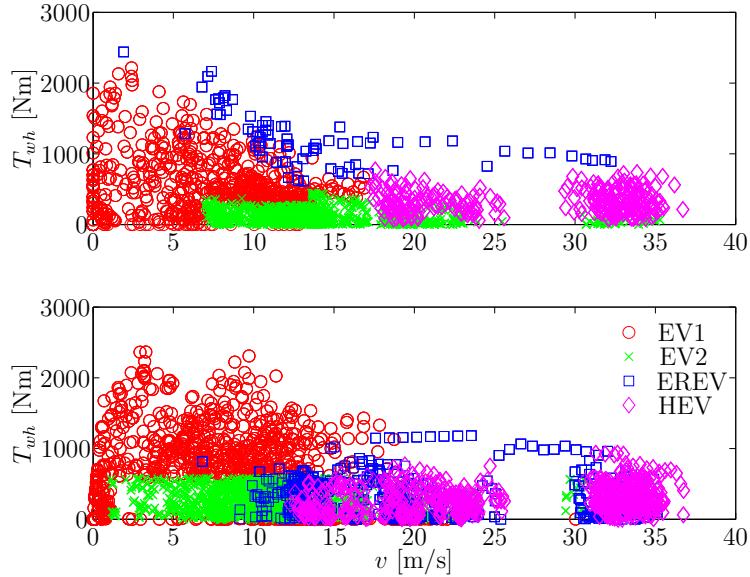


Figure 15: Aachen cycle, powertrain modes, HOT (top) and S1.

and memory use

2. a comparison between heuristic and optimal control-based techniques: generally speaking the latter outperform the rule-based approach under the same unpredictable circumstances, particularly in terms of fuel economy; however, heuristic algorithms can also achieve good performance, yet they require a higher amount of tuning and they are less robust to system variations
3. a comparison between different implementations of optimal-control-based techniques (ECMS): map-based ECMS induce lower computing efforts but higher memory use, while the opposite is true for vector-based ECMS
4. a comparison between online solutions and a globally optimal solution calculated off line with a prior knowledge of the driving profile: if properly designed, online energy managers can be very close to global optimum in terms of fuel economy.

The software developed for this benchmark will be made available on the web site [www.ecosm12.org](http://www.ecosm12.org) for further use by control engineering students and professionals that desire to test their own energy management solutions.

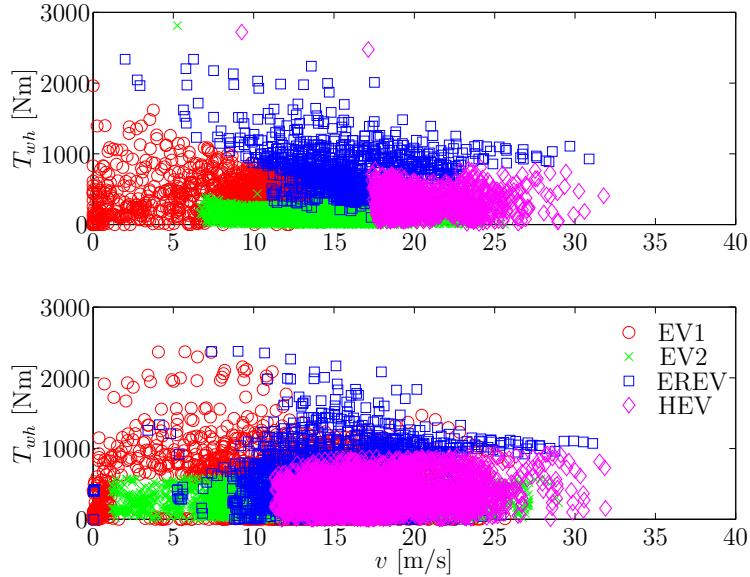


Figure 16: Arco–Merano cycle, powertrain modes, HOT (top) and S1.

A parametric PMP algorithm, HOT, will be also accessible to calculate a global optimum reference. Such platform could be enriched in the future with generators of random but realistic driving profiles and the possibility of modifying the structure and the components of the powertrain in the online-running model representing the actual system.

### Acknowledgements

The prize awarded to the winning team was made available by IFP School with the support of the Tuck Foundation. The correct conduct of the benchmark has been guaranteed by the jury members, whose support has been thorough and valuable: Chris Manzie (Univ. of Melbourne), Urs Christen (Ford Aachen), and Andreas Ehinger (IFP Energies nouvelles and Tuck Foundation), besides A. Sciarretta and P. Tona.

### References

- [1] Baumann, B., Rizzoni, G., & Washington, G. (1998) Intelligent Control of Hybrid Vehicles Using Neural Networks and Fuzzy Logic, SAE Paper 981061.

- [2] Brahma, A., Guezennec, Y., & Rizzoni, G. (2000) Optimal Energy Management in Series Hybrid Electric Vehicles, in Proc. of the American Control Conference, 60–64.
- [3] Paganelli, G., Guerra, T.M., Delprat, S., Santin, J.J., Combes, E., & Delhom, M. (2000) Simulation and Assessment of Power Control Strategies for a Parallel Hybrid Car, Journal of Automobile Engineering 214, 705–718.
- [4] Salman, M., Schouten, N.J., & Kheir, N.A. (2000) Control Strategies for Parallel Hybrid Vehicles, in Proc. of the American Control Conference, 524–528.
- [5] Lin, C.C., Kang, J.M., Grizzle, J.W., & Peng, H. (2001) Energy Management Strategy for a Parallel Hybrid Electric Truck, in Proc. of the American Control Conference, 2878–2883.
- [6] Kleimaier, A. & Schroder, D. (2002) An Approach for the Online Optimized Control of a Hybrid Powertrain, in Proc. of the 7th International Workshop on Advanced Motion Control.
- [7] Sciarretta, A., Back, M., & Guzzella, L. (2004) Optimal Control of Parallel Hybrid Electric Vehicles, IEEE Transactions on Control Systems Technology, 12(3), 352–363.
- [8] Koot, M., Kessels, J., de Jager, B., Heemels, W., van den Bosch, P., & Steinbuch, M. (2005) Energy Management Strategies for Vehicular Electric Power Systems, IEEE Transactions on Vehicle Technology, 54(3), 1504–1509.
- [9] Sciarretta, A. & Guzzella, L. (2007) Control of Hybrid Electric Vehicles, IEEE Control Systems Magazine, 27(2), 60–70.
- [10] Hofman, T., Ebbesen, S., & Guzzella, L. (2012) Topology Optimization for Hybrid Electric Vehicles with Automated Transmissions, IEEE Transactions on Vehicular Technology, 61(6), 2442–2451.
- [11] Hofman, T., Steinbuch, M., Serrarens, A., van Druten, R. (2008) Rule-Based Equivalent Consumption Minimization Strategies for Hybrid Vehicles, in Proc. of the 17th IFAC World Congress.

- [12] Ambühl, D., Sciarretta, A., Onder, C., Guzzella, L., Sterzing, S., Mann, K., Kraft, D., & Küsell, M. (2007). A Causal Operation Strategy for Hybrid Electric Vehicles Based on Optimal Control Theory, in Proc. of the 4th Braunschweig Symposium on Hybrid Vehicles and Energy Management.
- [13] Serrao, L., Onori, S., & Rizzoni, G. (2009) ECMS as a Realization of Pontryagin's Minimum Principle for HEV Control, in Proc. of the American Control Conference, 3964–3969.
- [14] Kim, N.W., Cha, S.K., & Peng, H. (2011) Optimal Control of Hybrid Electric Vehicles Based on Pontryagin's Minimum Principle, IEEE Transactions On Control Systems Technology, 19(5) 1279-1287.
- [15] van Berkel, K., Hofman, T., Vroemen, B., & Steinbuch, M. (2012) Optimal Control of a Mechanical-Hybrid Powertrain, IEEE Transactions on Vehicular Technology, 61(2), 485–497.
- [16] Musardo, C. & Rizzoni, G. (2005) A-ECMS: An Adaptive Algorithm for Hybrid Electric Vehicle Energy Management, Proc. of the IEEE Conference on Decision and Control and the European Control Conference, 1816–1823.
- [17] Pisù, P. & Rizzoni, G. (2007) A Comparative Study of Supervisory Control Strategies for Hybrid Electric Vehicles, IEEE Transactions On Control Systems Technology, 15(3), 506–518.
- [18] Sivertsson, M., Sundström, C., & Eriksson, L. (2011) Adaptive Control of a Hybrid Powertrain with Map-based ECMS, Proc. of the IFAC World Congress.
- [19] Anatone, M., Cipollone, R., Donati, A., & Sciarretta, A. (2005) Control-Oriented Modeling and Fuel Optimal Control of a Series Hybrid Bus, SAE Paper 2005-01-1163.
- [20] Pisù, P. & Rizzoni, G. (2005) A Supervisory Control Strategy for Series Hybrid Electric Vehicles With two Energy Storage Systems, in Proc. of the IEEE Conference on Vehicle Power and Propulsion.

- [21] Cipollone, R. & Sciarretta, A. (2006) Analysis of the Potential Performance of a Combined Hybrid Vehicle with Optimal Supervisory Control, in Proc. of the IEEE Int. Conference on Control Applications.
- [22] Liu, J.M. & Peng, H. (2006) Control Optimization for a Power-Split Hybrid Vehicle, Proc. of the American Control Conference.
- [23] Borhan, H.A. & Vahidi, A. (2010) Model Predictive Control of a Power-Split Hybrid Electric Vehicle with Combined Battery and Ultracapacitor Energy Storage, proc. of the American Control Conference, 5031–5036.
- [24] O'Kneefe, M. & Markel, T. (2006) Dynamic Programming Applied to Investigate Energy Management Strategies for a Plug-in HEV, in Proc. of the 22nd Internatinal Battery, Hybrid and Fuel Cell Electric Vehicle Symposium and Exposition.
- [25] Tulpule, P., Marano, V., & Rizzoni, G. (2009) Effects of Different PHEV Control Strategies on Vehicle Performance, Proc. of the American Control Conference.
- [26] Larsson V., Johannesson, L., & Egardt, B. (2010) Impact of Trip Length Uncertainty on Optimal Discharging Strategies for PHEVs, in Proc. of the IFAC Symposium on Advances in Automotive Control, 2010.
- [27] Stockar, S., Marano, V., & Canova, M. (2011) Energy-Optimal Control of Plug-in Hybrid Electric Vehicles for Real-World Driving Cycles, IEEE Transactions On Vehicular Technology, 60(7) 2949-2962.
- [28] Serrao, L., Sciarretta, A., Grondin, O., Chasse, A., Creff, Y., di Domenico, D., Pognant-Gros, P., Querel, C., & Thibault, L. (2013) Open Issues in Supervisory Control of Hybrid Electric Vehicles: A Unified Approach Using Optimal Control Methods, Oil & Gas Science and Technology, ahead of print.
- [29] Spencer, B.F., Dyke, S.J., & Deoskar, H.S. (1998), Benchmark problems in structural Control: Part I – Active Mass Driver System, Earthquake Engineering and Structural Dynamics, 27(11), 1127–1139.
- [30] Yasui, Y. (2012), JSCE-SICE Benchmark Problem 2: Fuel Consumption Optimization of Commuter Vehicle using Hybrid Powertrain, in Proc. of World Congress on Intelligent Control and Automation, 606–611.

- [31] Guzzella, L. & Sciarretta, A. (2013), Vehicle Propulsion Systems, Introduction to Modeling and Optimization, Springer, Chapter 2, p. 13–45.
- [32] Falières, Q., Grasset, O., Roblet, K., Xu, Y., Noiret, C., Serrao, L., & Sciarretta, A. (2011) A Contradictory Analysis of GM Voltec Powertrain, in Proc. of the European Electric Vehicle Congress.
- [33] Grebe, U.D. & Nite, L.T. (2011), VOLTEC – The Propulsion System for Chevrolet Volt and Opel Ampera, ATZ Autotechnology, 5(2011), 4.
- [34] Miller, M.A., Holmes, A.G., Conlon, B.M., & Savagian, P.J. (2011) The GM Voltec 4ET50 Multi-Mode Electric Transaxle, SAE Paper 2011-01-0887.
- [35] Parrish, R., Elankumaran, K., Gandhi, M., Nance, B. et al., (2011), Voltec Battery Design and Manufacturing, SAE Paper 2011-01-1360.
- [36] Do, D.V. (2010), Diagnostic de batteries lithium-ion dans des applications embarquées, PhD Thesis, Université de Technologie de Compiègne.
- [37] TNO Report (2006), Review and Analysis of the Reduction Potential and Costs of Technological and Other Measures to Reduce CO<sub>2</sub> Emissions from Passenger Cars.
- [38] International Energy Agency report (2011), CO<sub>2</sub> Emissions from Fuel Combustion: Highlists.
- [39] Marcos, D. & Bordons, C. (2012), Power Management of a Plug-in Hybrid Electric Vehicle Based on Cycle Energy Estimation, in Proc. of the 2012 IFAC Workshop on Engine and Powertrain Control, Simulation, and Modeling.
- [40] Sivertsson, M. (2012) Adaptive Control Using Map-Based ECMS for a PHEV, in Proc. of the 2012 IFAC Workshop on Engine and Powertrain Control, Simulation, and Modeling.
- [41] Onori, S., Serrao, L., & Rizzoni, G. (2010) Adaptive Equivalent Consumption Minimization Strategy for HEVs, in Proc. of the ASME Dynamic Systems and Control Conference.

- [42] Chasse, A. & Sciarretta, A. (2011), Supervisory Control of Hybrid Powertrains: an Experimental Benchmark of Offline Optimization and Online Energy Management, *Control Engineering Practice*, 19(11), 1253–1265.
- [43] Merz, F., Sciarretta, A., Dabadie, J.-C., & Serrao, L. (2012) On the Optimal Thermal Management of Hybrid-Electric Vehicles with Heat Recovery Systems, *Oil & Gas Science and Technology*, 67(4), 610–612.